Probability of success in biomedical research

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Program for today/course objectives

Objectives:

- Understand how to obtain a probability of success estimate for a research project
- Ability to discuss various success criteria and their pros and cons
- Understand how to interpret and use a probability of success estimate

Program:

- Mix of lectures and exercises discussion as we go along is very welcome!
- Two coffee breaks (morning and afternoon) and a lunch break in between

Consider how the material might apply to your own research and share if you like.



Case study

Loosely based on a real case

A drug is being developed to treat migraine

We have performed a small proof of concept study with positive results

Now we wish to design a large confirmatory trial to confirm that the drug works





Design of the proof of concept study

A double-blind, parallel group, placebo controlled trial



FERRING PHARMACEUTICALS

Results from the proof of concept study

A positive study



Significant difference at week 4 of -2 (SE=0.89) MMD on high dose compared to pbo (p=0.01)



Placebo

Standard deviation of CFB in MMD to week 4 of 6.5



Based on Results Posted | A Study With Lu AG09222 in Adults With Migraine Who Have Not Been Helped by Prior Preventive Treatments | ClinicalTrials.gov (data after 4 weeks is fictional)

SE = Standard Error

For Internal Use - Internal

Study design for the confirmatory trial

A double-blind, parallel group, placebo controlled trial



Distribution of the difference in means

Suppose patients are randomised to one of two treatments, with n_i patients allocated to Treatment *i*

Suppose that the *j*th patient receiving Treatment *i* will yield a continuous response y_{ij} with $Y_{ij} \sim N(\mu_i, \sigma_i)$, independent.

Then the distribution of the difference in means
$$\bar{y}_1 - \bar{y}_0 = \frac{1}{n_1} \sum_{i=1}^{n_1} y_{1i} - \frac{1}{n_0} \sum_{i=1}^{n_0} y_{0i}$$
 is
 $\bar{y}_1 - \bar{y}_0 \sim N(\mu_1 - \mu_0, \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_0^2}{n_0}})$
Where $\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_0^2}{n_0}}$ simplifies to $\sigma \sqrt{\frac{2}{n}}$ in case $\sigma_1 = \sigma_0$ and $n_1 = n_0$.



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Deciding on a sample size

Power calculation (continuous endpoint, assuming known variance)

 H_0 : null hypothesis - no effect H_1 : alternative hypothesis – the effect equals δ μ_0 : true mean CFB in MMD on placebo μ_1 : true mean CFB in MMD on drug σ : standard deviation of CFB in MMD β : level at which to control the false negative rate α : level at which to control the false positive rate Z_q : qth quantile of the standard normal distribution

The sample size can be calculated by finding

n such that $0 + Z_{1-\alpha}\sigma\sqrt{\frac{2}{n}} = \delta + Z_{\beta}\sigma\sqrt{\frac{2}{n}}$: $n = \frac{2\sigma^2 (Z_{1-\alpha} + Z_{1-\beta})^2}{2\sigma^2}$



SE = Standard Error For Internal Use - Internal

Exercise 1 – propose a sample size for the confirmatory trial

You are very welcome to work together

Requirements/assumptions:

- We would like to have a power of 90%
- We would like to control the false positive rate at a one-sided 2.5% level
- Make appropriate assumptions about:
 - the expected difference δ in mean CFB in MMD at week 12
 - the standard deviation σ for the CFB in MMD at week 12

Hints:

- make use of the results from the proof of concept study
- In R Z_q can be obtained using qnorm (q) and x^2 by x^2

